

3rd WORKSHOP ON PARTICLE PHYSICS

NATIONAL CENTRE FOR PHYSICS
(QUAID-I-AZAM UNIVERSITY)

Detectors for High Energy Physics

Lecture III - Tracking

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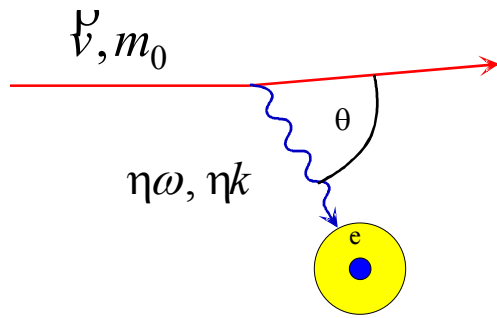
Detection of particles

Particles are detected through their interaction with the detector

In the following we will study in a quantitative way the interaction of charged and neutral particles with matter

Charged particle through matter

- Scatter on nuclei ($m \ll M_{\text{nucleus}}$) without losing energy
- Loose energy interacting with atomic electrons ($m_e \ll m$) without changing direction



$$\left\langle \frac{dE}{dx} \right\rangle = - \int_0^\infty NE \frac{d\sigma}{dE} \eta d\omega$$

N : electron density

If $h\omega$ is large enough the atom is ionized

Instead of ionizing an atom, under certain conditions the photon can also escape from the medium.

> Emission of Cherenkov and Transition radiation.

Scattering

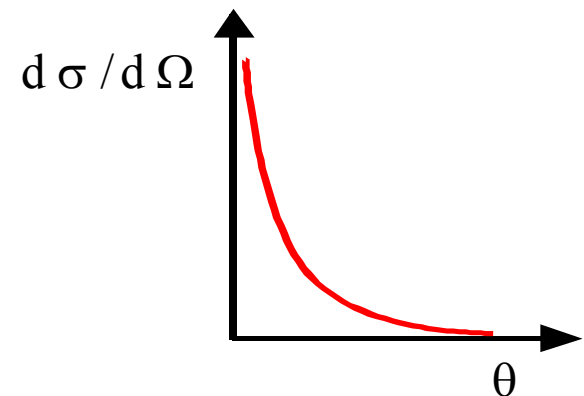
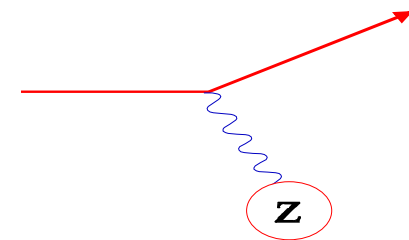
An incoming particle with charge z interacts with a target of nuclear charge Z . The cross-section for this e.m. process is

$$\frac{d\sigma}{d\Omega} = 4 z^2 Z^2 r_e^2 \left(\frac{m_e c}{\beta p} \right)^2 \frac{1}{\sin^4 \theta / 2} \quad \langle \theta \rangle = 0$$

Rutherford formula

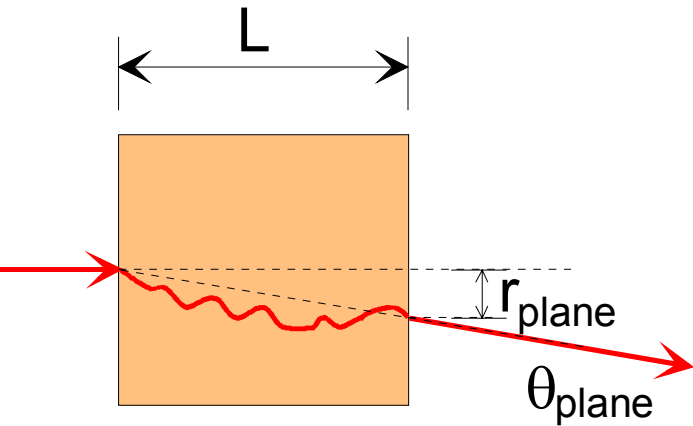
Average scattering angle

Cross-section for $\theta \rightarrow 0$ infinite !



Multiple Scattering

Sufficiently thick material layer \rightarrow the particle will undergo multiple scattering.

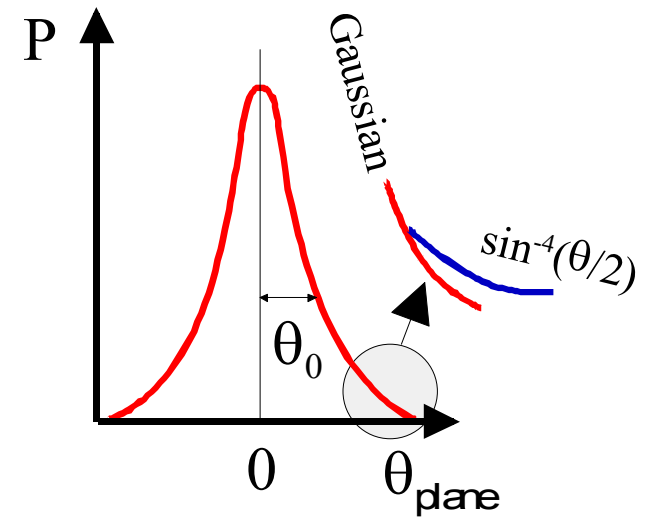


$$\theta_0 = \theta_{plane}^{RMS} = \sqrt{\langle \theta_{plane}^2 \rangle} = \frac{1}{\sqrt{2}} \theta_{space}^{RMS}$$

Approximation :

X_0 is radiation length of the medium

$$\theta_0 \propto \frac{1}{p} \sqrt{\frac{L}{X_0}}$$



Multiple scattering contribution to momentum error

$$\frac{\sigma(p)}{p_T} \propto \sigma(x) \cdot p_T \quad \text{and} \quad \sigma(x)|^{MS} \propto \theta_0 \propto \frac{1}{p} \quad \Longrightarrow \quad \left. \frac{\sigma(p)}{p_T} \right|^{MS} = \text{constant}$$

independent of p !

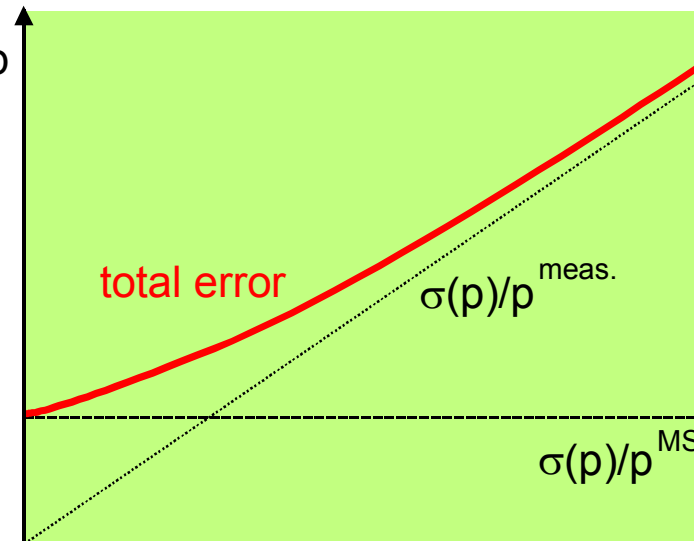
More precisely:

$$\left. \frac{\sigma(p)}{p_T} \right|^{MS} = \frac{0.045}{B(T) \sqrt{L(m) X_0(m)}}$$

$\sigma(p)/p$

ex: Ar ($X_0=110\text{m}$), $L=1\text{m}$, $B=1\text{T}$

$$\left. \frac{\sigma(p)}{p_T} \right|^{MS} \approx 0.5\%$$



energy loss by ionization: Bethe-Bloch

$$\left\langle \frac{dE}{dx} \right\rangle = -4\pi N_A r_e^2 m_e c^2 z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2 m_e c^2 \gamma^2 \beta^2}{I^2} T_{\max} - \beta^2 - \frac{\delta}{2} \right]$$

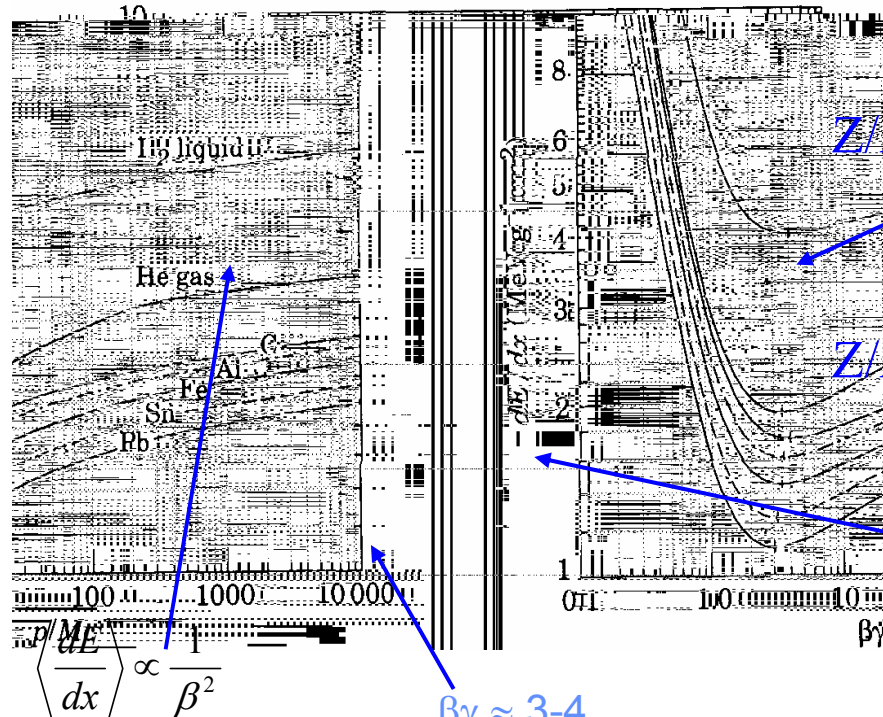
E/dx in [MeV g⁻¹ cm²]

Bethe-Bloch formula only valid for “heavy” particles ($m \geq m_\mu$).

E/dx depends only on β ,
independent of m !

first approximation:
medium simply
characterized by

$\frac{Z}{A}$
~ electron density



$Z/A = 1$

“Fermi plateau”

$Z/A \sim 0.5$

$\left\langle \frac{dE}{dx} \right\rangle \propto \ln \beta^2 \gamma^2$

“relativistic rise”

$\beta\gamma \approx 3-4$

minimum ionizing particles, MIPs

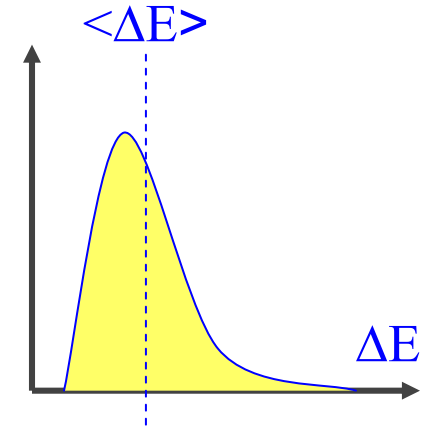
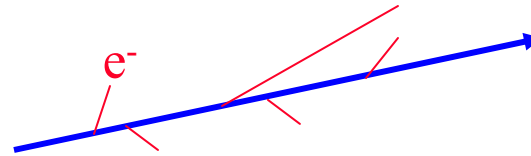
“kinematical term”

Landau tails

For **thin layers** (and low density materials):

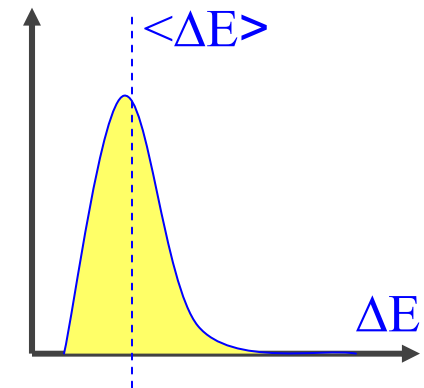
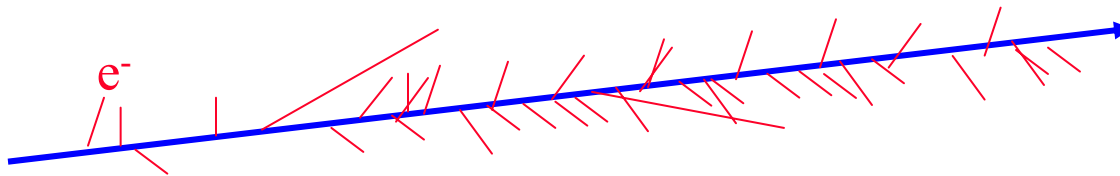
- Few collisions, some with high energy transfer.
- Energy loss distributions show large fluctuations towards high losses:

"Landau tails"



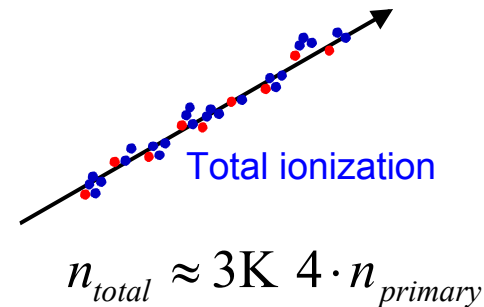
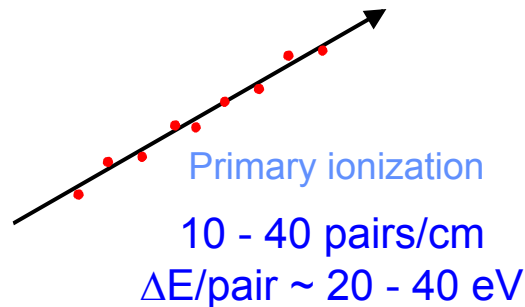
For **thick layers** and high density materials:

- Many collisions.
- Central Limit Theorem → Gaussian shape distributions.



Ionization in Gas

Often the resulting primary electron will have enough kinetic energy to ionize other atoms.

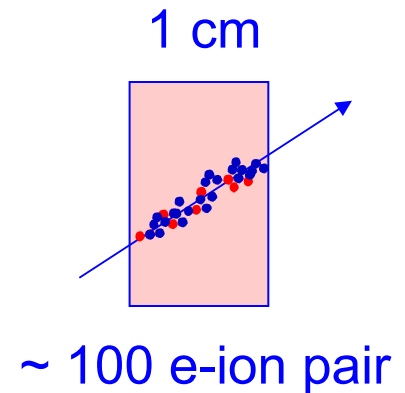


Assume detector, 1 cm thick, filled with Ar gas:

100 electron-ion pairs are not easy to detect!

Noise of amplifier $\approx 1000 \text{ e}^-$ (ENC) !

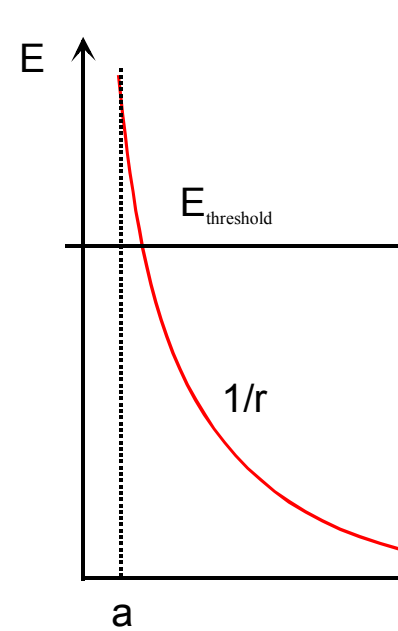
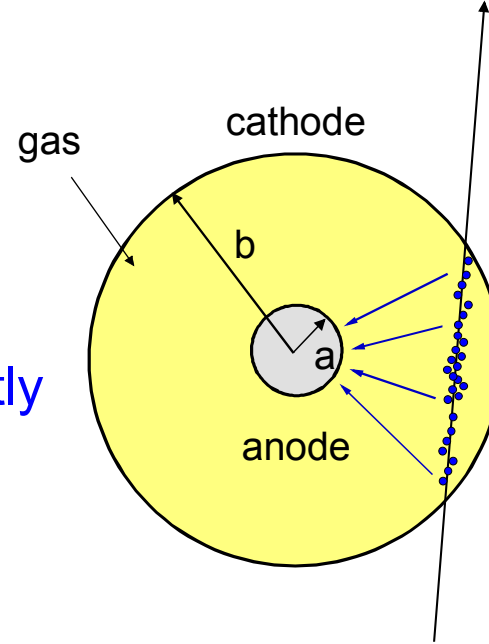
We need to increase the number of e-ion pairs.



Amplification in gas

Electrons drift towards the anode wire

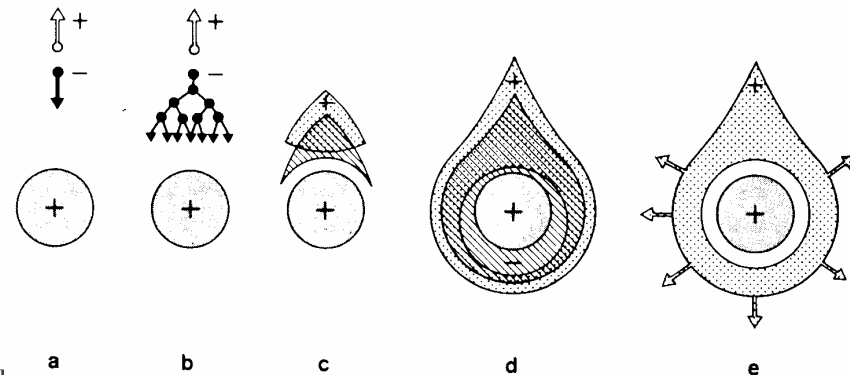
Close to the anode wire the field is sufficiently high (some kV/cm), so that e^- gain enough energy for further ionization → exponential increase of number of e^- -ion pairs.



$$E(r) = \frac{CV_0}{2\pi\epsilon_0} \cdot \frac{1}{r}$$

$$V(r) = \frac{CV_0}{2\pi\epsilon_0} \cdot \ln \frac{r}{a}$$

Avalanche formation within a few wire radii and within $t < 1$ ns!

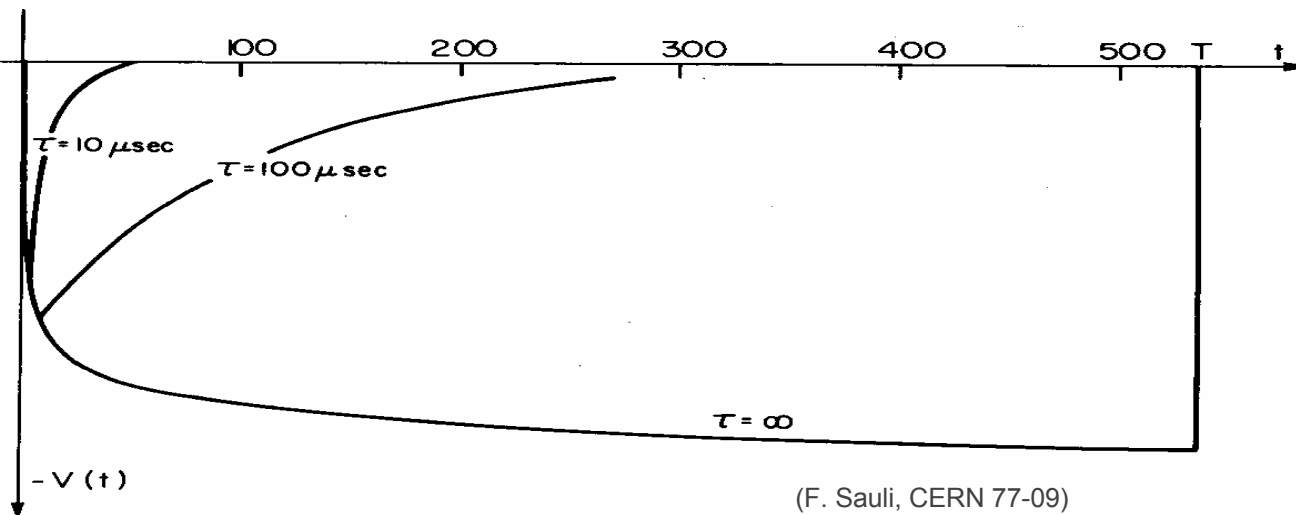


Signal formation

Signal induction both on anode and cathode due to moving charges (both electrons and ions).

Electrons collected by anode wire, i.e. dr is small (few μm). Electrons contribute only very little to detected signal (few %).

$$dv = \frac{Q}{lCV_0} \frac{dV}{dr} dr$$

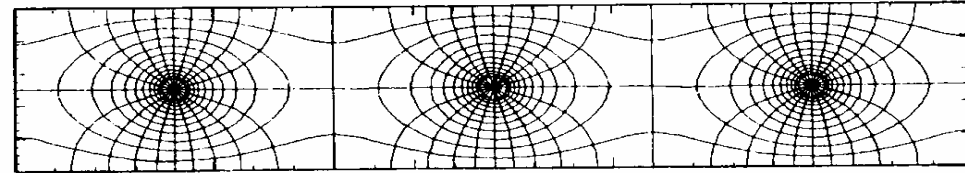
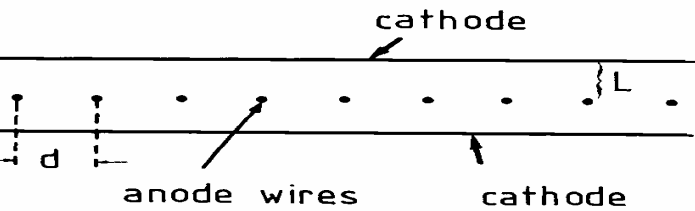


Ions have to drift back to cathode i.e. dr is big. Signal duration limited by total ion drift time !

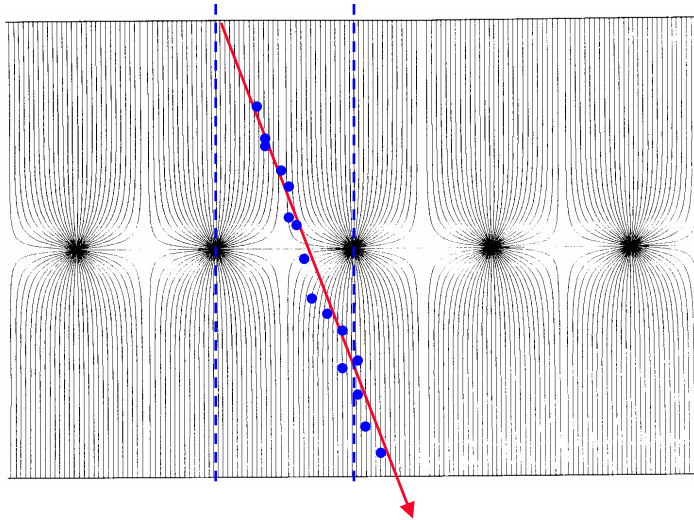
Need electronic signal differentiation to limit dead time.

Multi wire proportional chambers

(G. Charpak et al. 1968, Nobel prize 1992)



field lines and equipotentials around anode wires



Typical parameters:

$L=5\text{mm}$, $d=1\text{mm}$,

$a_{\text{wire}}=20\text{mm}$.

Normally digital readout:
spatial resolution limited to

$$\sigma_x \approx \frac{d}{\sqrt{12}}$$

($d=1\text{mm}$,
 $\sigma_x=300\ \mu\text{m}$)

Multi wire proportional chambers

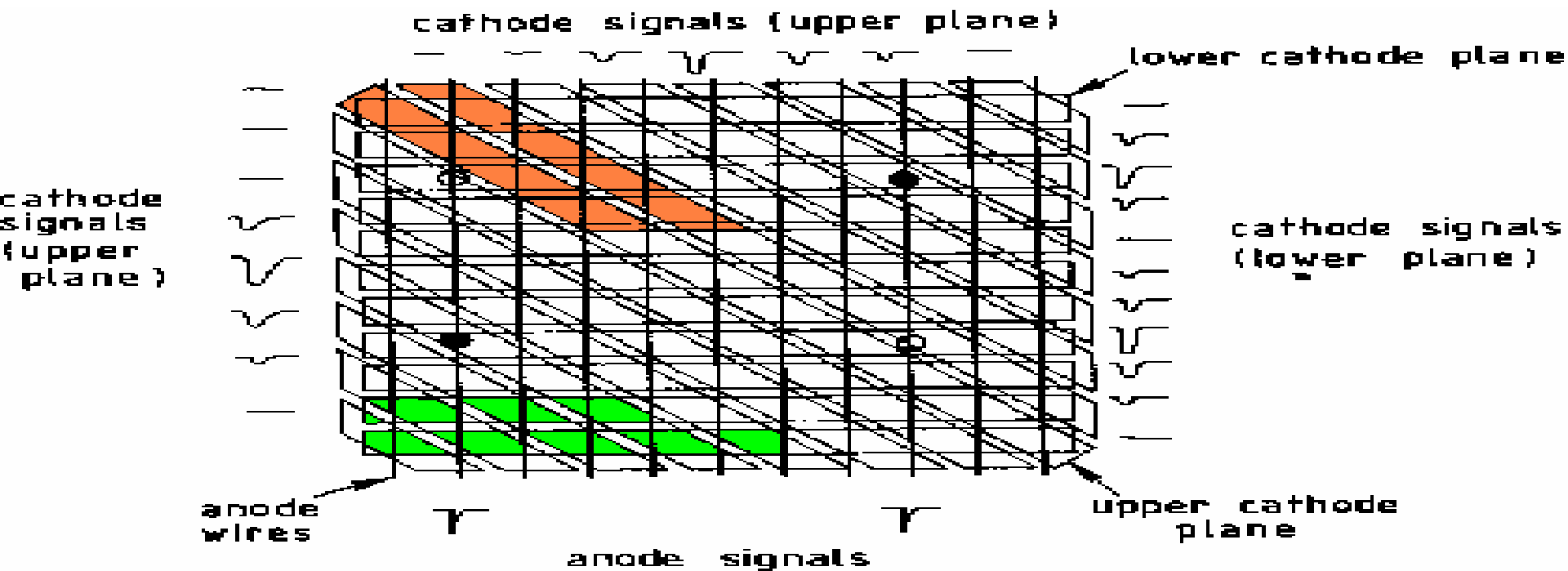
Measuring the coordinate by induction

Example: 1 wire plane

+ 2 segmented cathode planes

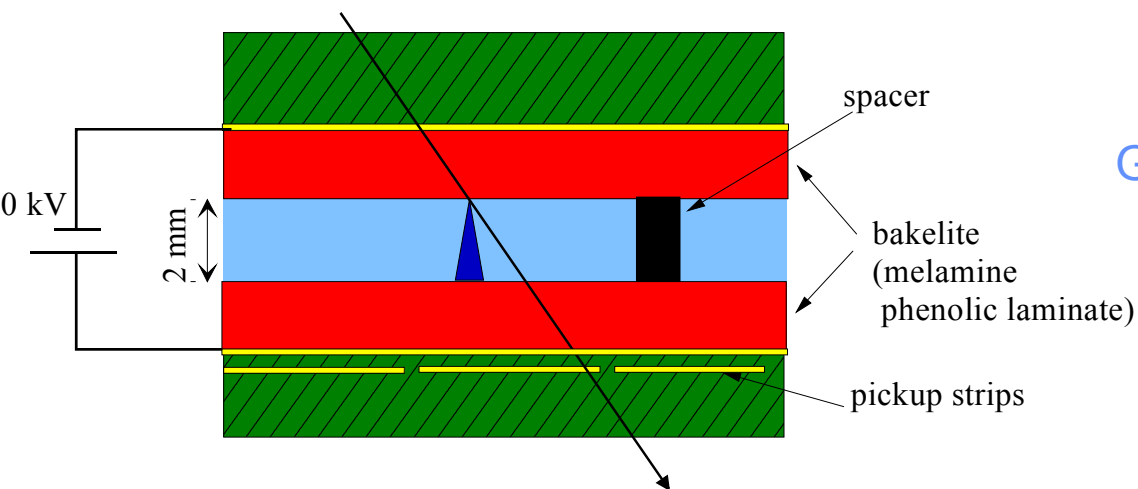
Analog readout of cathode planes.

→ $\sigma \approx 100 \mu\text{m}$



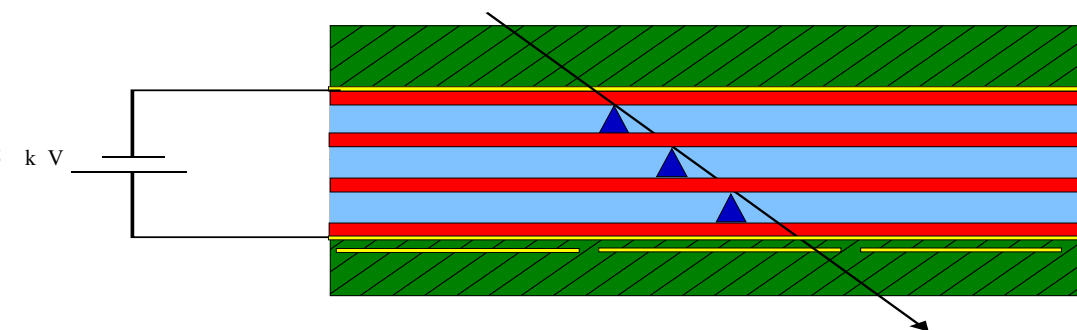
Resistive plate chambers (RPC)

No wires !



Gas: $C_2F_4H_2$, (C_2F_5H) + few % isobutane

Time dispersion $\approx 1..2$ ns \rightarrow suited as trigger chamber
Rate capability ≈ 1 kHz / cm^2

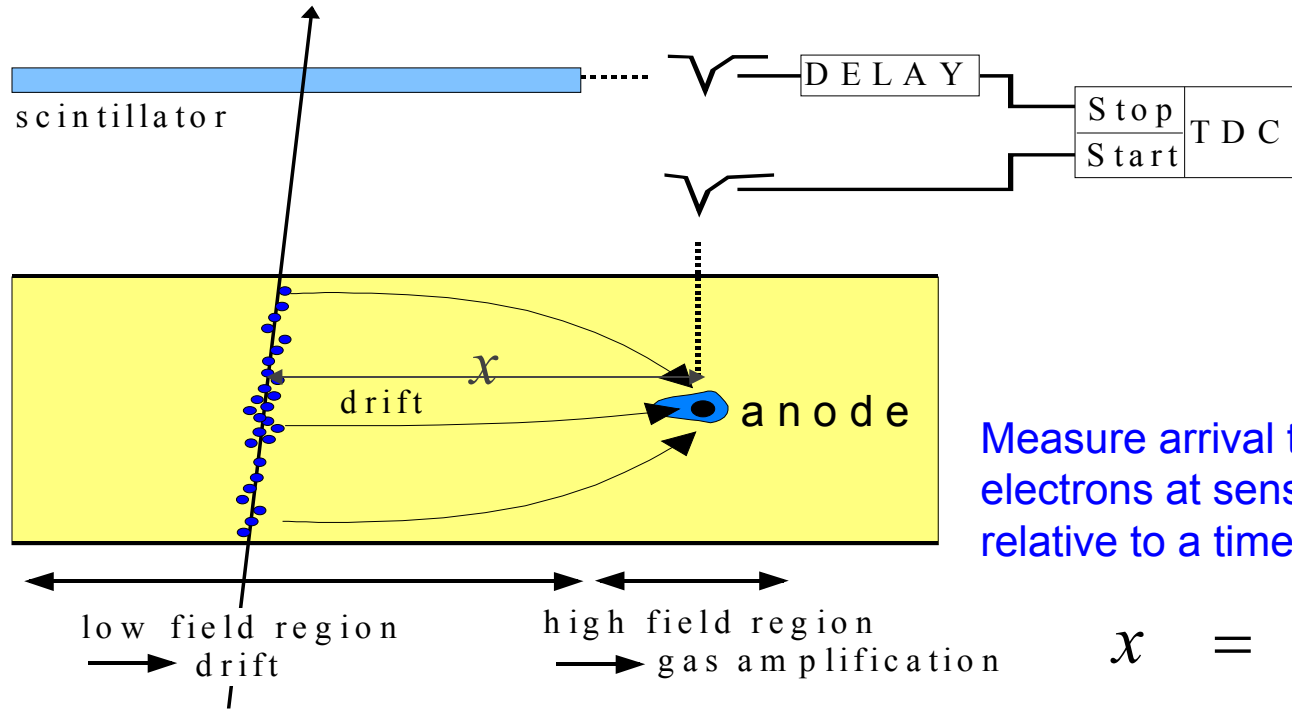


Double and multigap geometries \rightarrow improve timing and efficiency

Problem: Operation close to streamer mode.

Drift chambers

First studies: T. Bressani, G. Charpak, D. Rahm, C. Zupancic, 1969
 First operation drift chamber: A.H. Walenta, J. Heintze, B. Schürlein, NIM 92 (1971) 373)



Measure arrival time of electrons at sense wire relative to a time t_0 .

$$x = \int v_D(t) dt$$

What happens during the drift towards the anode wire ?

- ☞ Diffusion ?
- ☞ Drift velocity ?

Drift and diffusion in gases

No external fields:

Electrons and ions will lose their energy due to collisions with the gas atoms → thermalization

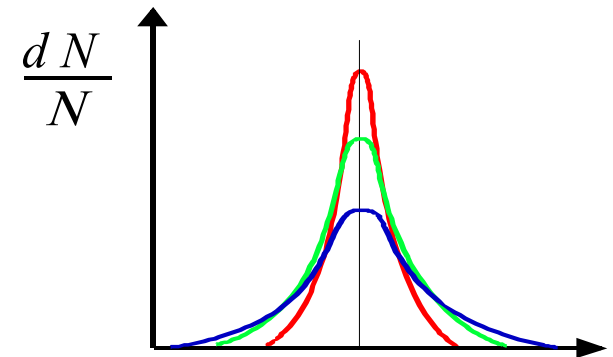
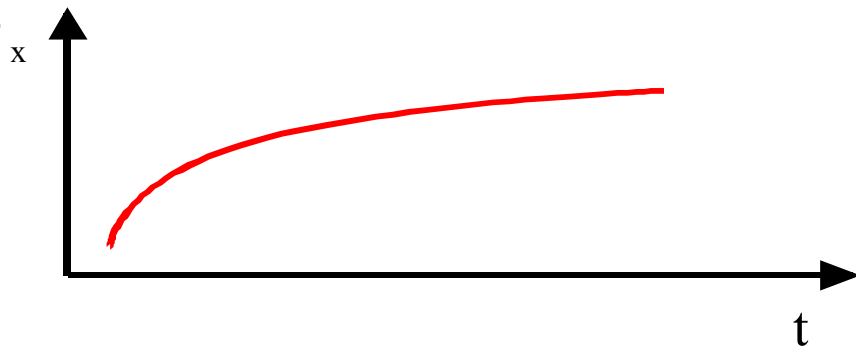
$$\varepsilon = \frac{3}{2} kT \approx 40 \text{ meV}$$

Undergoing multiple collisions, an originally localized ensemble of charges will diffuse

$$\frac{dN}{N} = \frac{1}{\sqrt{4\pi Dt}} e^{-(x^2/4Dt)} dx$$

$$\sigma_x(t) = \sqrt{2Dt} \quad \text{or} \quad D = \frac{\sigma_x^2(t)}{2t}$$

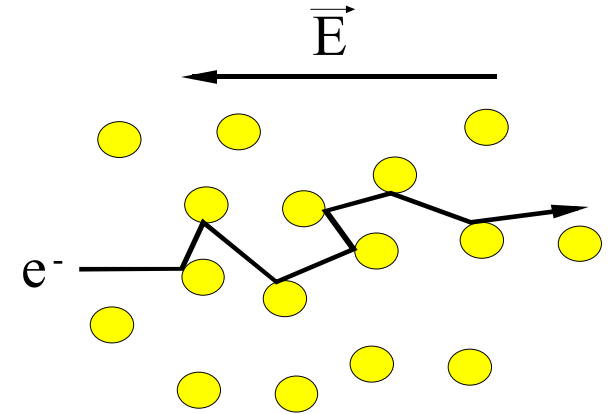
D: diffusion coefficient



Drift and diffusion in gases

External electric field

“stop and go” traffic due to scattering
from gas atoms → drift



$$\mathbf{v}_D = \mu \mathbf{E}$$

$$\mu = \frac{e \tau}{m} \quad (\text{mobility})$$

the equilibrium ...

λ_ε : fractional energy loss / collision

$$\frac{x}{v_D \tau} \lambda_\varepsilon \varepsilon = eEx$$

$$\tau = \frac{1}{N \sigma v} \quad v: \text{instantaneous velocity}$$

Time needed to move by x

Drift and diffusion in gases

in the equilibrium ...

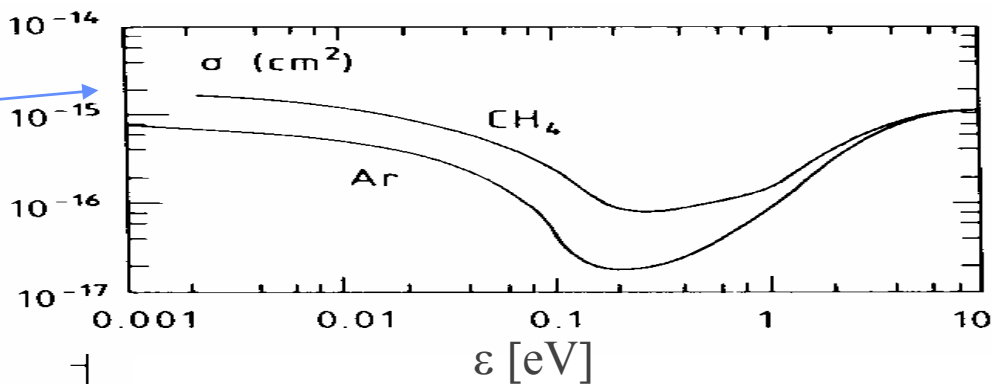
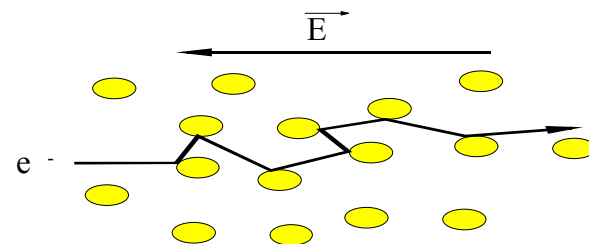
$$\frac{x}{v_D \tau} \lambda_\epsilon \epsilon = eEx$$

λ_ϵ : fractional energy loss / collision
 $\tau = \frac{1}{N \sigma v}$: instantaneous velocity

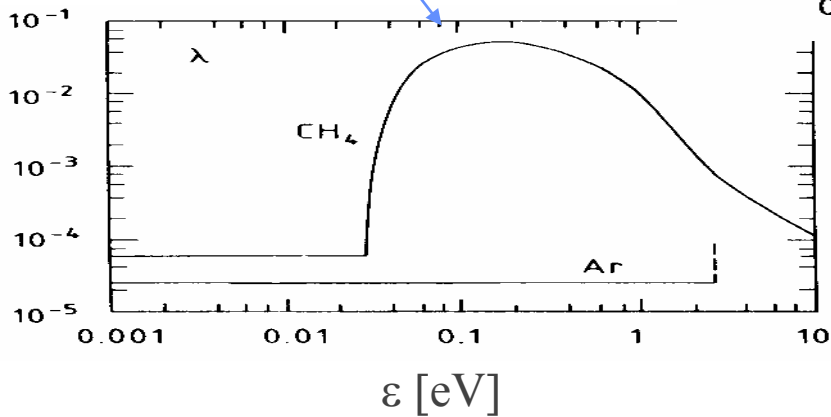
$$\vec{v}_D = \frac{eE}{mN \sigma} \sqrt{\frac{\lambda}{2}}$$

$\sigma = \sigma(\epsilon) !$

$\lambda = \lambda(\epsilon) !$



(B. Schmidt, thesis, unpublished, 1986)



Typical electron drift velocity: **5 cm/μs** Ion drift velocities: ca. 1000 times smaller

Drift and diffusion in gases

In the presence of **electric and magnetic fields**, drift and diffusion are driven by $\vec{E} \times \vec{B}$ effects

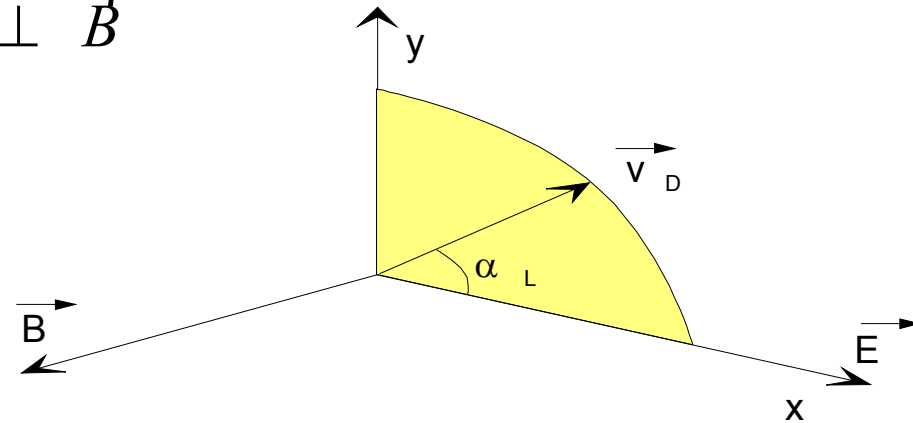
Look at 2 special cases:

Special case: $\vec{E} \perp \vec{B}$

$$\tan \alpha_L = \omega \tau$$

α_L : Lorentz angle

$$\omega = \frac{e B}{m} \quad \text{cyclotron frequency}$$



$$\vec{v}_D \parallel \vec{E}$$

Drift and diffusion in gases

Special case:

$$\vec{E} \parallel \vec{B}$$

The longitudinal diffusion (along B-field) is unchanged.

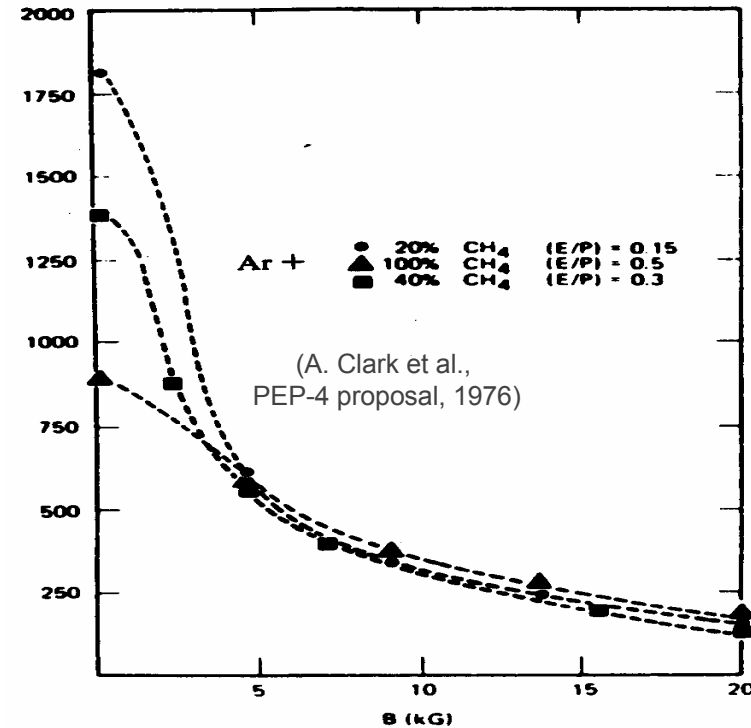
In the transverse projection the electrons are forced on circle segments with the radius v_T/ω .

The transverse diffusion coefficient appears reduced

$$D_T(B) \approx \frac{D_0}{1 + \omega^2 \tau^2}$$

Very useful... see later !

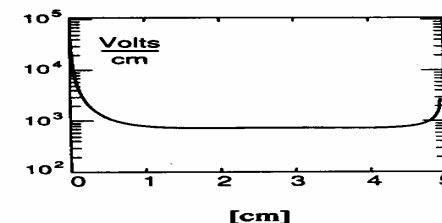
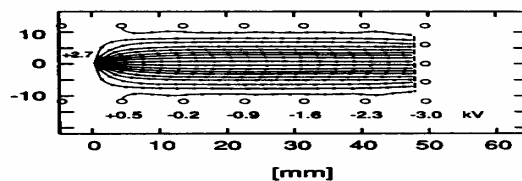
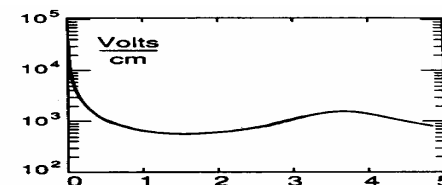
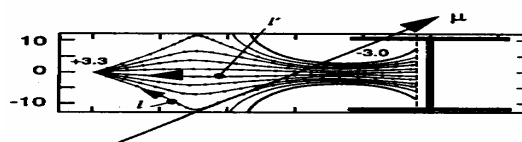
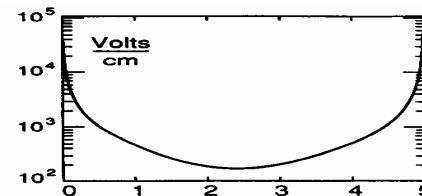
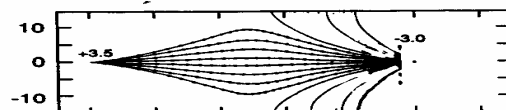
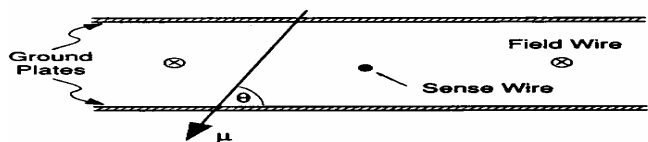
Transverse diffusion σ (μm) for a drift of 15 cm in different Ar/CH₄ mixtures



Drift chambers

Some planar drift chamber designs

Optimize geometry \rightarrow constant E-field
Choose drift gases with little dependence $v_D(E)$
 \rightarrow linear space - time relation $r(t)$



(U. Becker, in: Instrumentation in High Energy Physics, World Scientific)

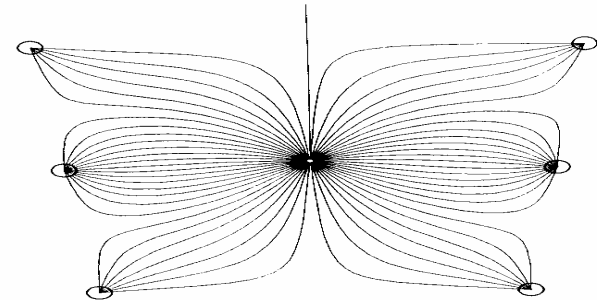
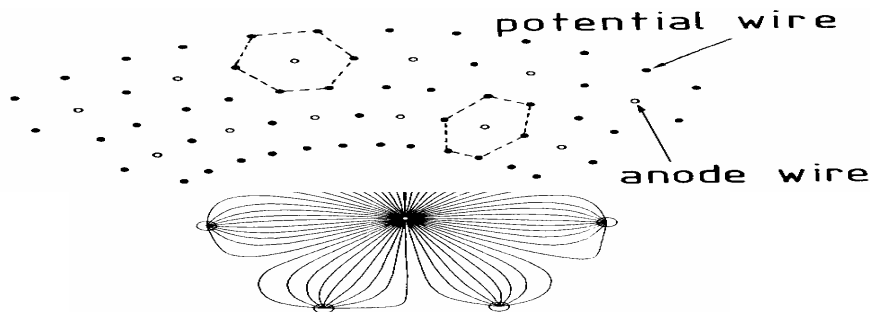
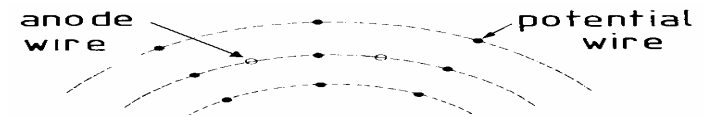
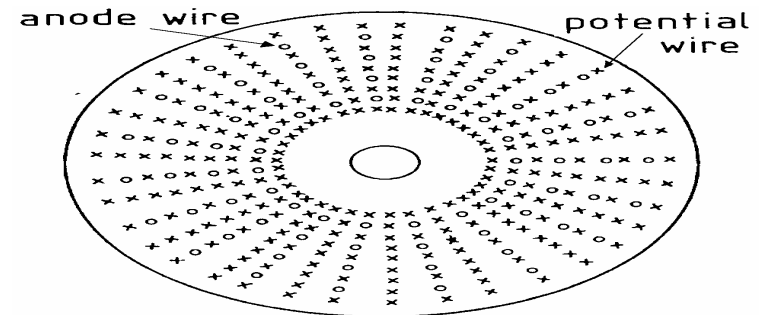
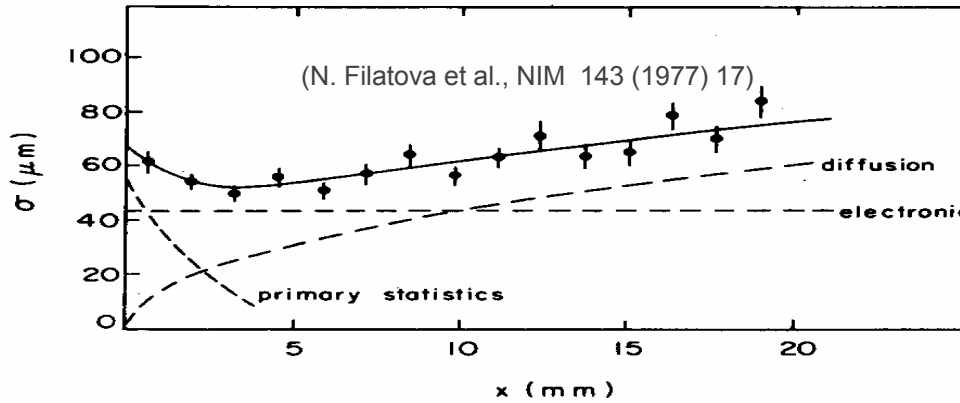
The spatial resolution is not limited by the cell size
 \rightarrow less wires, less electronics,
less support structure than in MWPC.

Drift chambers

Resolution determined by

- diffusion,
- path fluctuations,
- electronics
- primary ionization statistics

Various geometries of cylindrical drift chambers



Drift Chambers

Time Projection Chamber → full 3-D track reconstruction

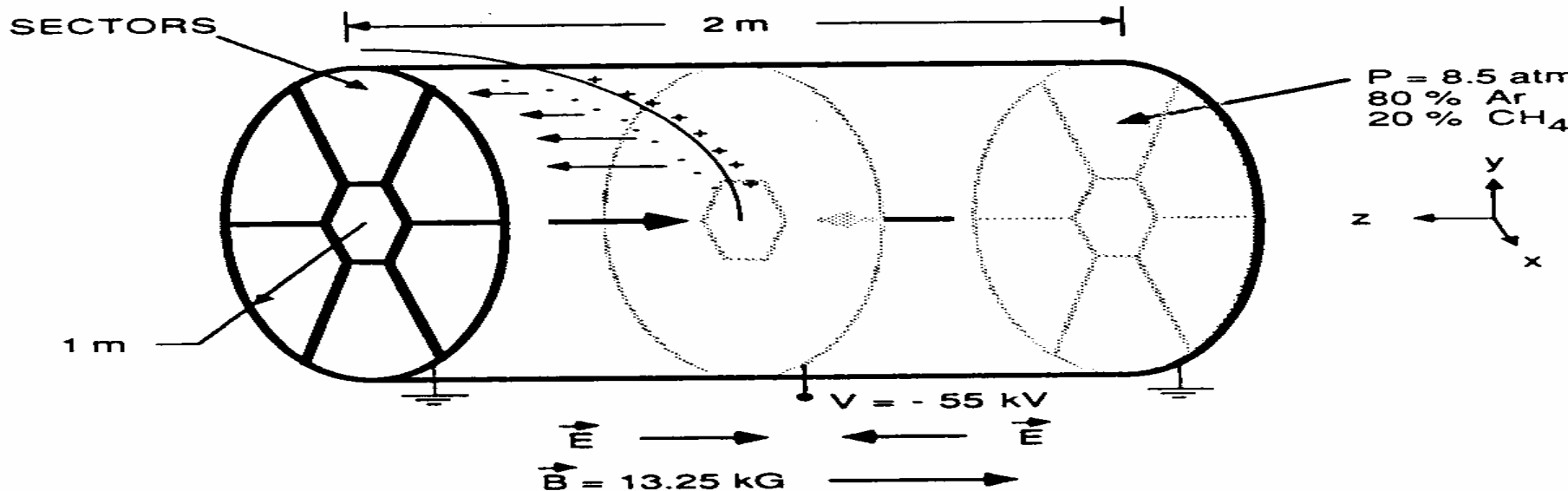
x-y from wires and segmented cathode of MWPC

z from drift time

in addition dE/dx information

Diffusion significantly reduced by B-field.

PEP-4 TPC



Drift Chambers

Drift over long distances \rightarrow very good gas quality required

Requires precise knowledge of $v_D \rightarrow$ LASER calibration + p, T corrections

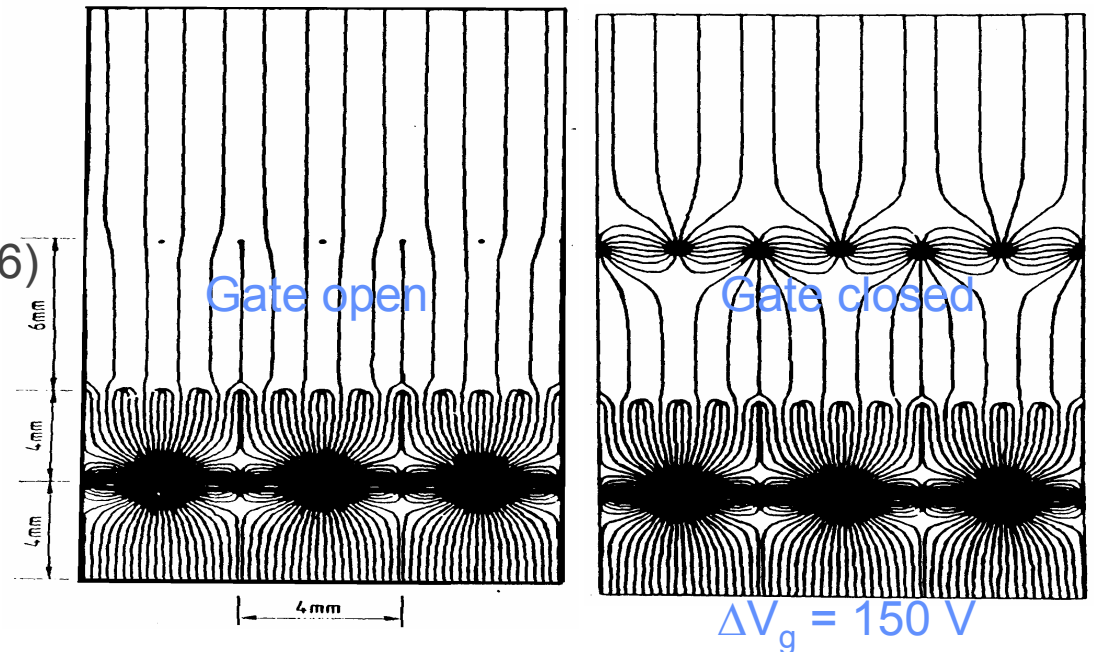
Space charge problem from positive ions, drifting back to midwall \rightarrow gating

ALEPH TPC

ALEPH coll., NIM A 294 (1990) 121,
Atwood et. Al, NIM A 306 (1991) 446)

\varnothing 3.6M, L=4.4 m

$\sigma_{R\phi} = 173 \mu\text{m}$
 $\sigma_z = 740 \mu\text{m}$
(isolated leptons)



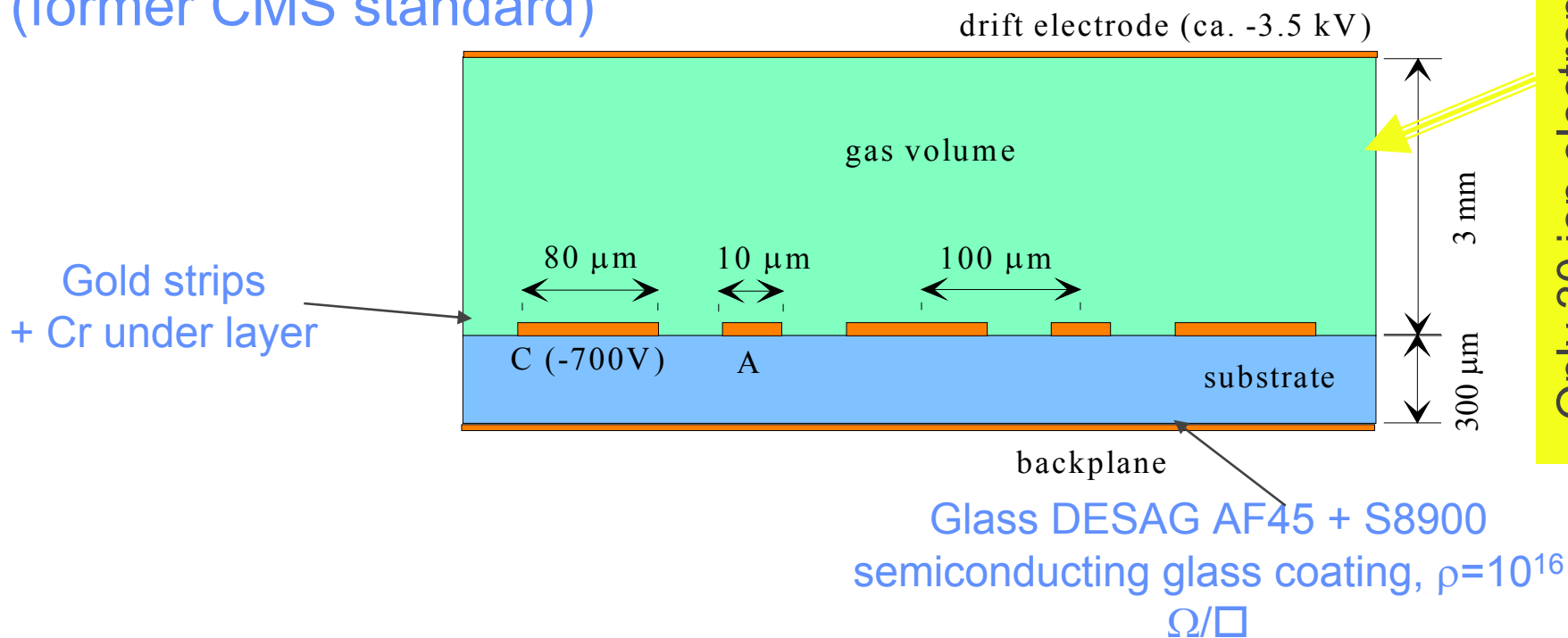
Micro gaseous detectors

Faster and more precision ? → smaller structures

(A. Oed, NIM A 263 (1988) 352)

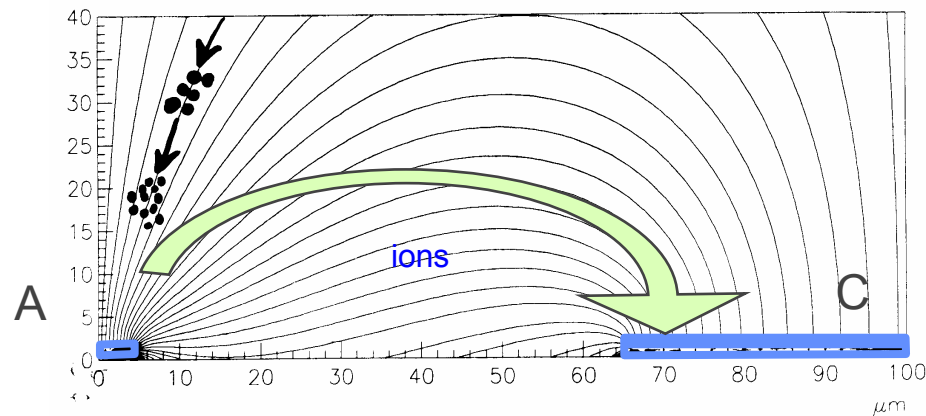
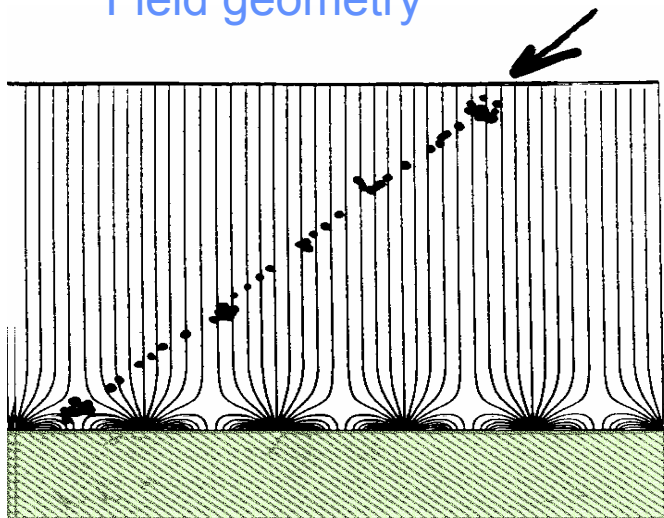
Microstrip gas chamber

geometry and typical dimensions
(former CMS standard)



Micro gaseous detectors

Field geometry



Fast ion evacuation → high rate capability
 $\approx 10^6 /(\text{mm}^2 \cdot \text{s})$

Gas: Ar-DME, Ne-DME (1:2), Lorentz angle 14° at 4T.

Gain $\leq 10^4$

Passivation: non-conductive protection of cathode edges

Resolution: $\approx 30..40 \mu\text{m}$

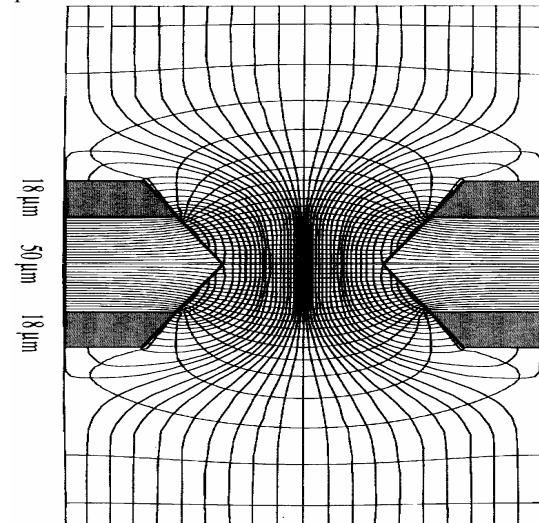
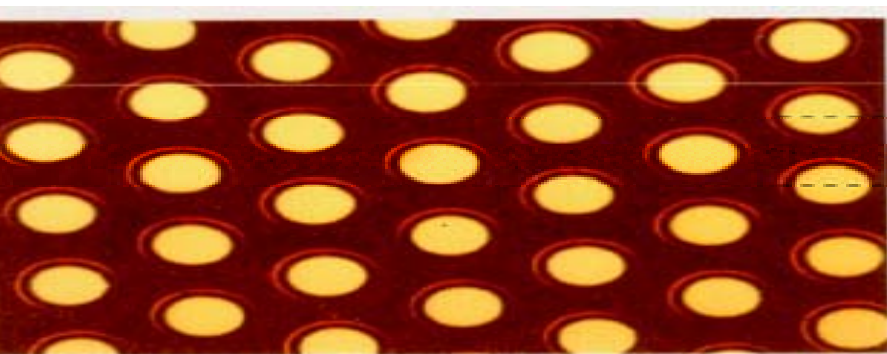
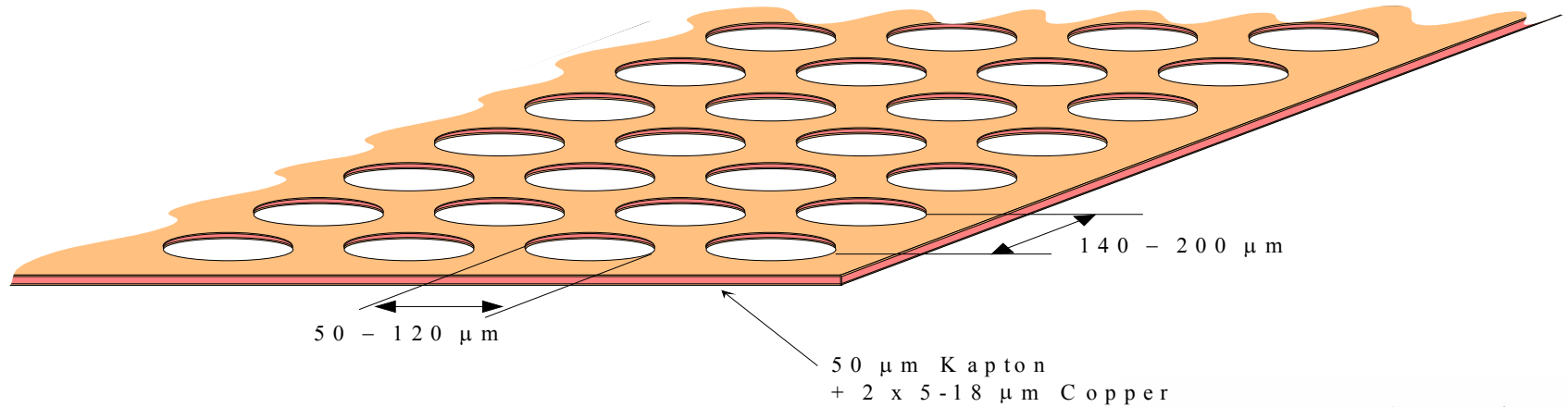
Aging: Seems to be under control.

10 years LHC operation $\approx 100 \text{ mC/cm}$

Micro gaseous detectors

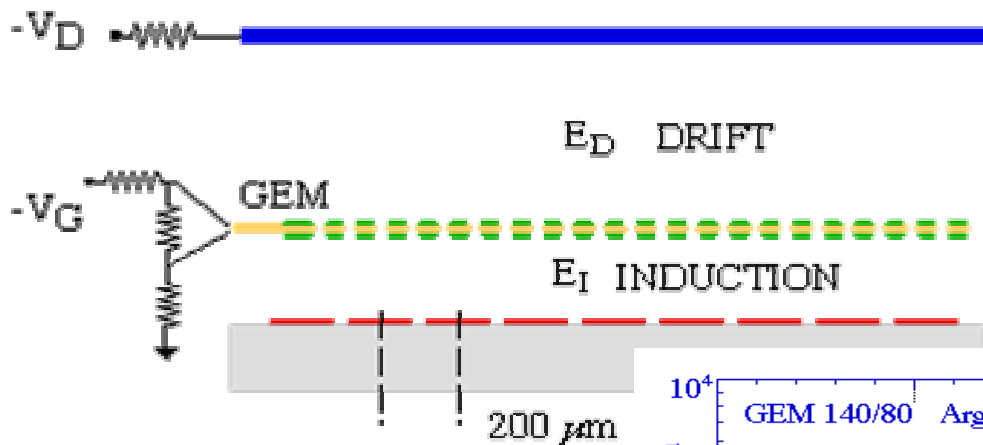
◆ GEM: The Gas Electron Multiplier

(R. Bouclier et al., NIM A 396 (1997) 50)

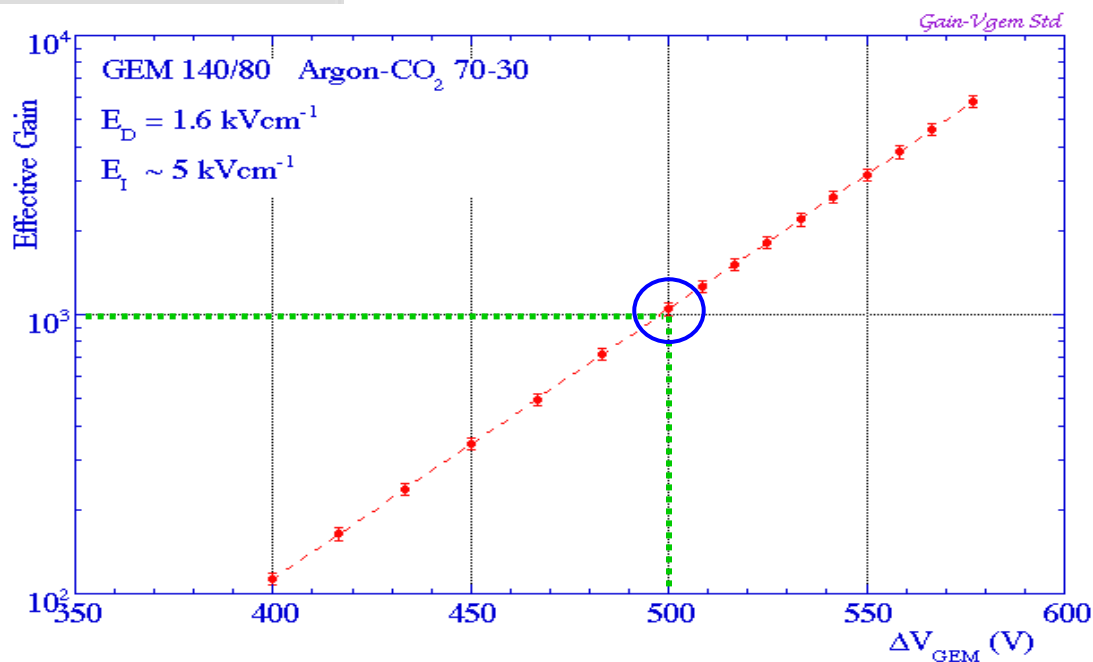


Micro photo of a GEM foil

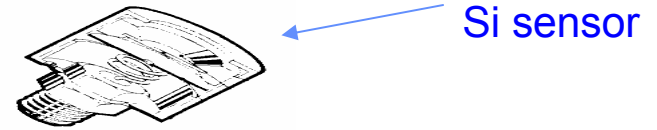
Micro gaseous detectors



Single GEM
+ readout pads



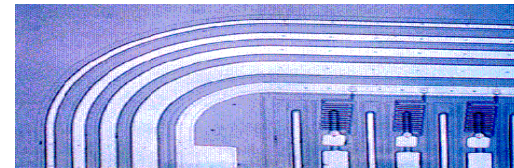
Silicon detectors



Silicon detectors

Solid state detectors have a long tradition for energy measurements (Si, Ge, Ge(Li)).

Here we are interested in their use as precision trackers !



ATLAS
SCT

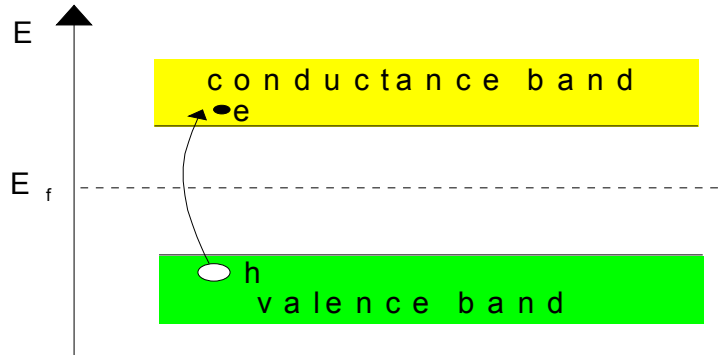
Silicon detectors

Some characteristic numbers for silicon

- 👉 Band gap: $E_g = 1.12 \text{ V}$.
- 👉 $E(\text{e-hole pair}) = 3.6 \text{ eV}$, ($\approx 30 \text{ eV}$ for gas detectors).
- 👉 High specific density (2.33 g/cm^3) $\rightarrow \Delta E/\text{track length for M.I.P.'s.: } 390 \text{ eV}/\mu\text{m} \approx 108 \text{ e-h}/\mu\text{m}$ (average)
- 👉 High mobility: $\mu_e = 1450 \text{ cm}^2/\text{Vs}$, $\mu_h = 450 \text{ cm}^2/\text{Vs}$
- 👉 Detector production by microelectronic techniques \rightarrow small dimensions \rightarrow fast charge collection ($< 10 \text{ ns}$).
- 👉 Rigidity of silicon allows thin self supporting structures. Typical thickness $300 \mu\text{m} \rightarrow \approx 3.2 \cdot 10^4 \text{ e-h}$ (average)
- 👉 **But: No charge multiplication mechanism!**

Silicon detectors

How to obtain a signal ?



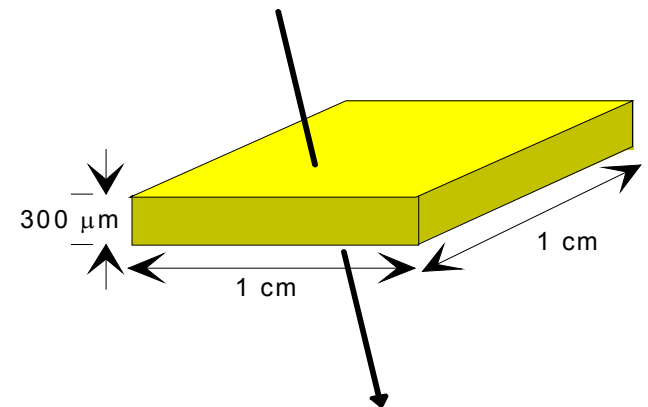
For Silicon: $n_i \approx 1.45 \cdot 10^{10} \text{ cm}^{-3}$

In this volume

we have $4.5 \cdot 10^8$ free charge carriers,
but only $3.2 \cdot 10^4$ e-h pairs produced by
a M.I.P.

→ Reduce number of free charge carriers,
i.e. deplete the detector

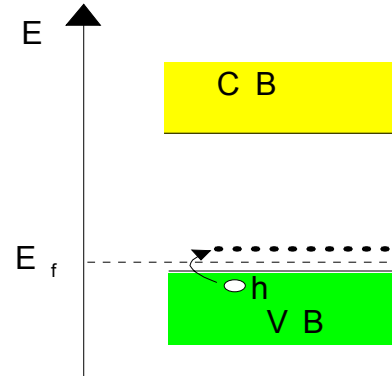
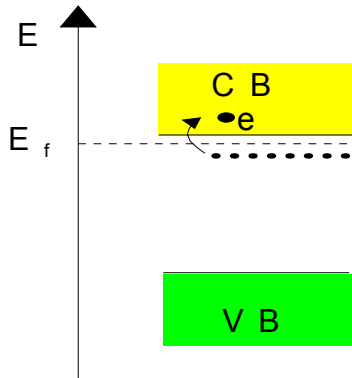
In a pure intrinsic (undoped)
material the electron density n and hole density p are
equal. $n = p = n_i$



Most detectors make use of reverse biased p-n junctions

Silicon detectors

Doping



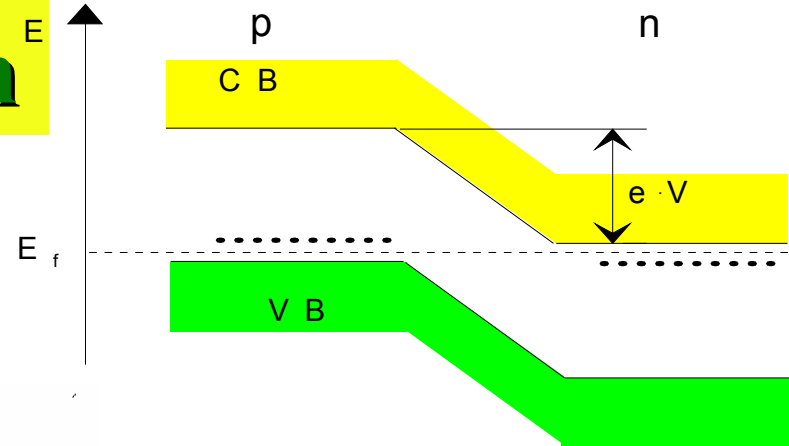
n-type: Add elements from Vth group, donors, e.g. As. Electrons are the majority carriers.

p-type: Add elements from IIIrd group, acceptors, e.g. B. Holes are the majority carriers.

	detector grade	electronics grade
doping concentration	$10^{12} \text{ cm}^{-3} \text{ (n)} - 10^{15} \text{ cm}^{-3} \text{ (p}^+)$	$10^{17(18)} \text{ cm}^{-3}$
resistivity	$\approx 5 \text{ k}\Omega \cdot \text{cm}$	$\approx 1 \Omega \cdot \text{cm}$

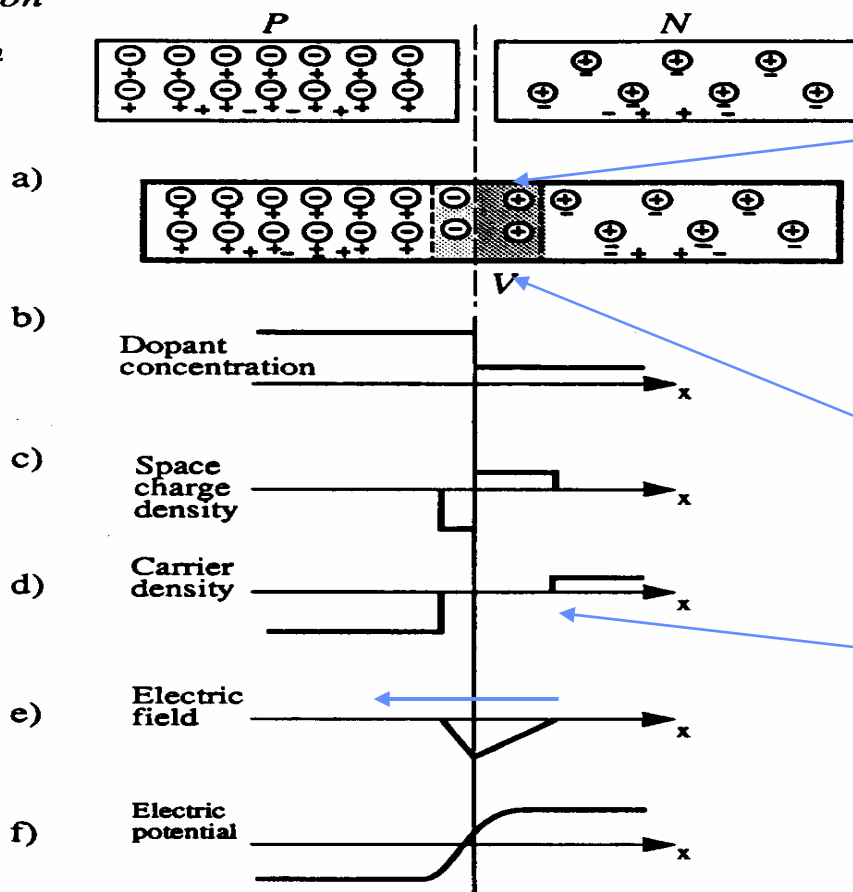
silicon detectors pn junction

There must be a single Fermi level!
 Deformation of band structure →
 potential difference.



⊖ Acceptor ion
 ⊕ Donor ion
 + Hole
 - Electron

THE PN JUNCTION



diffusion of e^- into p-zone, h^+ into n-zone
 → potential difference stopping diffusion

thin depletion zone

no free charge carriers
 in depletion zone

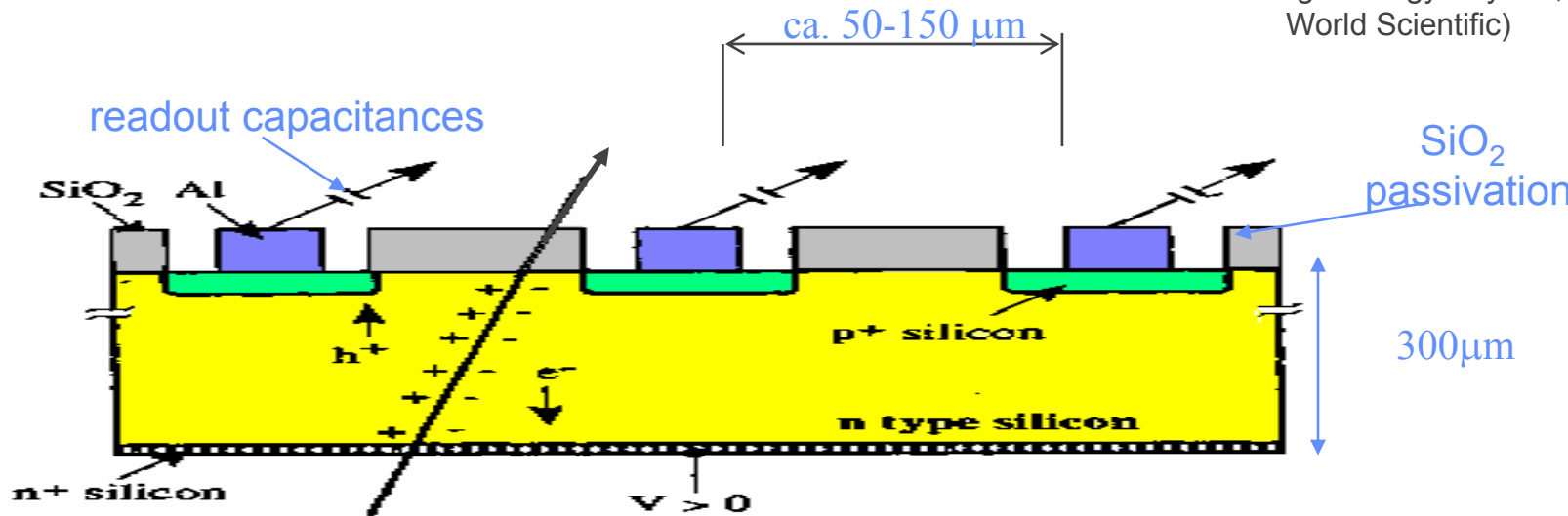
(A. Peisert, Instrumentation In High Energy Physics, World Scientific)

Silicon detectors

Spatial information by segmenting
the p doped layer →

- Application of a reverse bias voltage (about 100V) → the thin depletion zone gets extended over the full junction → fully depleted detector.
- Energy deposition in the depleted zone, due to traversing charged particles or photons (X-rays), creates free e⁻-hole pairs.
- Under the influence of the E-field, the electrons drift towards the n-side, the holes towards the p-side → detectable current.

(A. Peisert, Instrumentation
In High Energy Physics,
World Scientific)

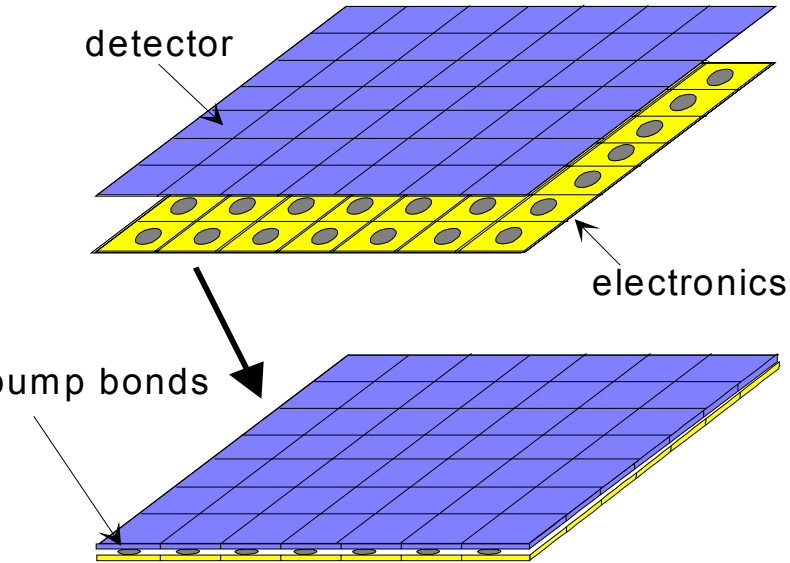


defines end of depletion zone
+ good ohmic contact

Silicon detectors

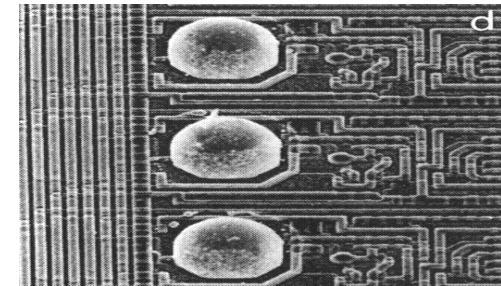
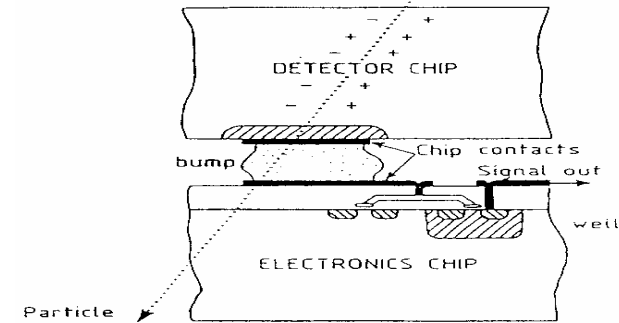
Silicon pixel detectors

- Segment silicon to diode matrix
- also readout electronic with same geometry
- connection by bump bonding technique



RD 19, E. Heijne et al., NIM A 384 (1994) 399

Flip-chip technique



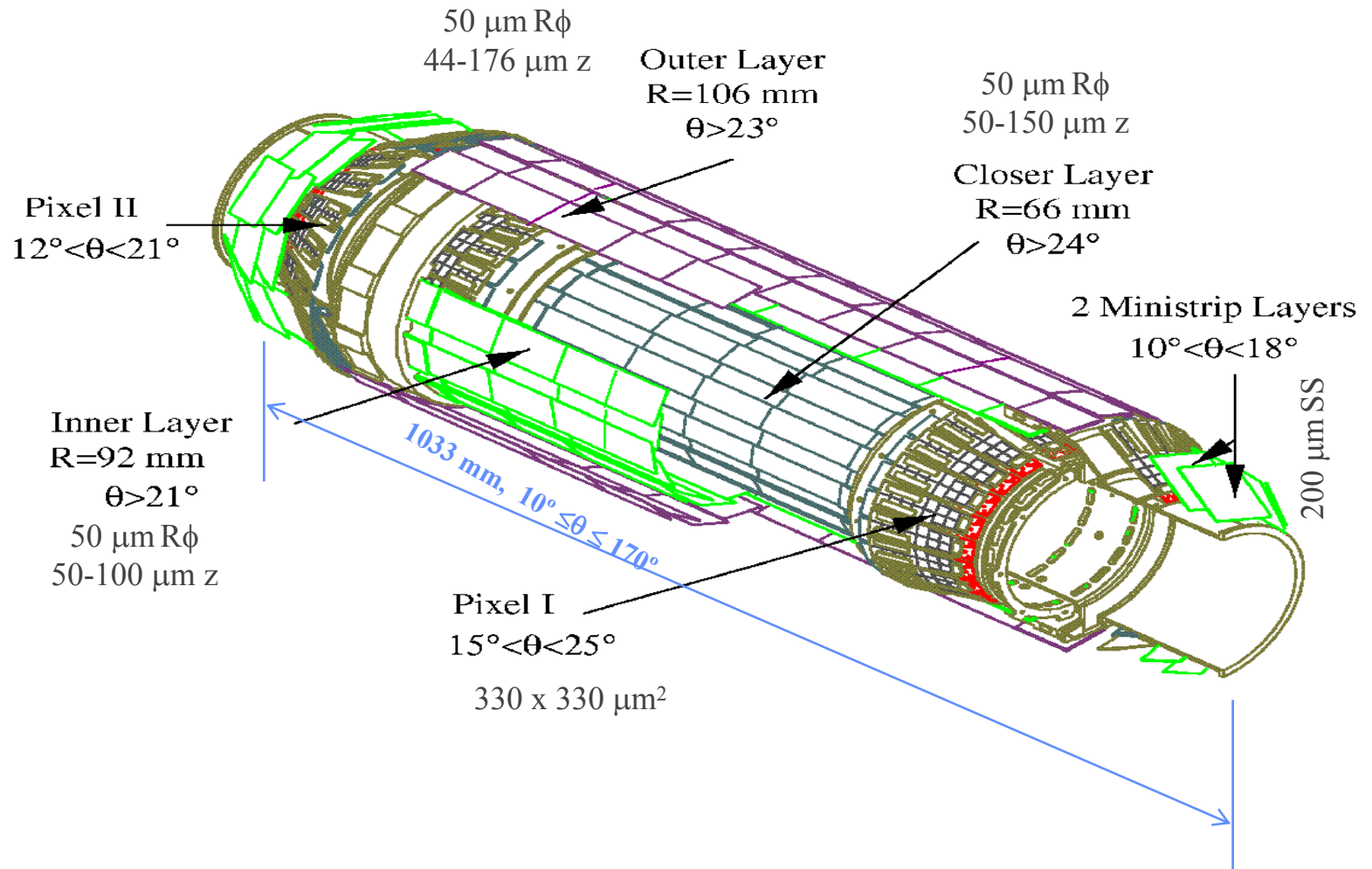
Requires sophisticated readout architecture

First experiment WA94 (1991), WA97
OMEGA 3 / LHC1 chip (2048 pixels,
50x500 mm²) (CERN ECP/96-03)

Pixel detectors will be used also in
LHC experiments (ATLAS, ALICE,
CMS)

Silicon Detectors

The DELPHI micro vertex detector (since 1996)



Silicon Detectors

about channels:

• 174 k strips, 1.2 M pixels

• total readout time: 1.6 ms

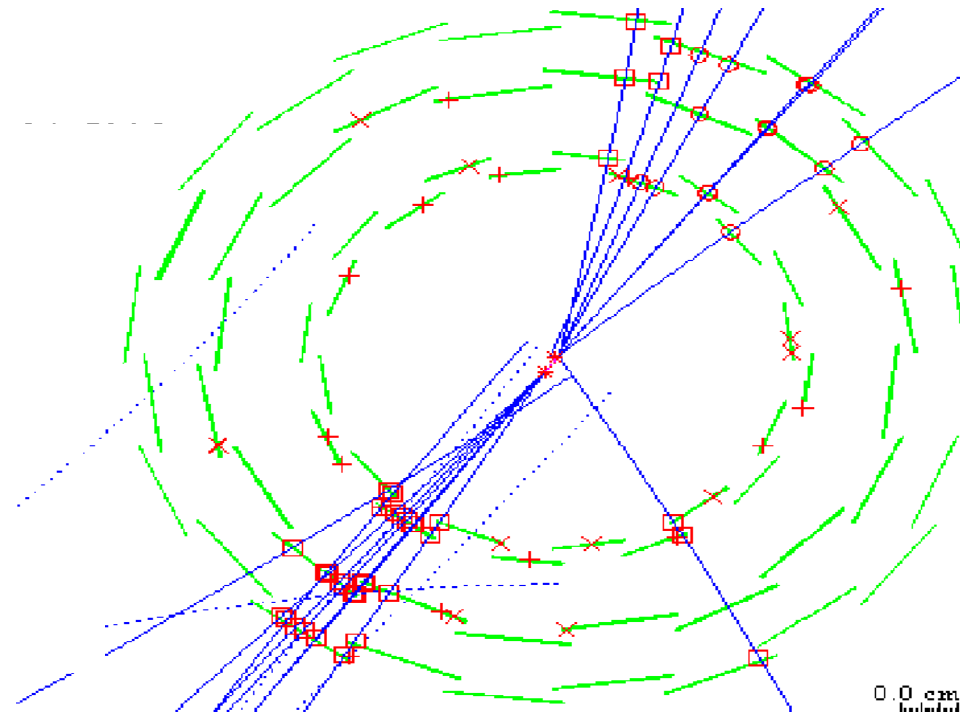
• total dissipated power 400 W →
• water cooling system

• point resolution in barrel part $\approx 10 \mu\text{m}$

• impact parameter resolution ($r\phi$)

$$28 \mu\text{m} \oplus 71 / \left(p \sin \frac{3}{2} \theta \right)$$

Delphi

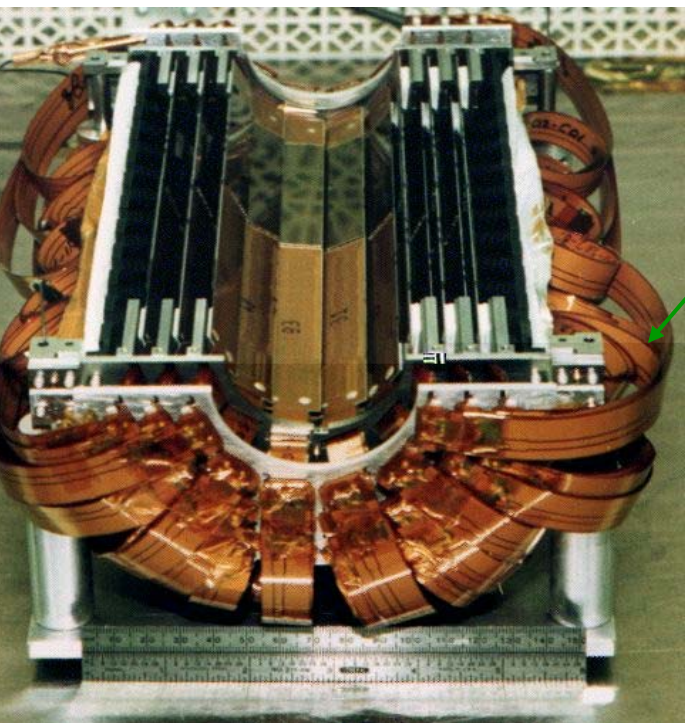


0.0 cm
0.0 cm

SLD Microvertex

Vertex detectors (CCD's, pixels):

- At **SLC**: inner radius **2.3 cm**, superior resolution.



SLD can do both b- and c-tagging with good purity.

